

Summary: Particle Kinetics

WHICH TOOL(s) TO USE?

Put effort up front deciding on which method(s) to use: *Newton*, *work/energy*, *linear impulse momentum* or *angular impulse momentum*. Use the Kinetics Table in Section 5.D of the lecture book as a guide.

THE FOUR-STEP PLAN: Follow it...it is your friend!

Method	Body model	Fundamental equations
Newton-Euler <i>(relating forces to accelerations)</i>	particle	$\sum \vec{F} = m\vec{a}$
	rigid body <i>(G = c.m. and A = any point on body)</i>	$\sum \vec{F} = m\vec{a}_G$ $\sum \vec{M}_A = I_A\vec{\alpha} + m\vec{r}_{G/A} \times \vec{a}_A$
Work-energy <i>(relating change in speed to change in position)</i>	particle	$T_1 + V_1 + U_{1 \rightarrow 2}^{(nc)} = T_2 + V_2$ where $T = \frac{1}{2}mv^2$
	rigid body <i>(G = c.m. and A = any point on body)</i>	$T_1 + V_1 + U_{1 \rightarrow 2}^{(nc)} = T_2 + V_2$ where $T = \frac{1}{2}mv_A^2 + \frac{1}{2}I_A\omega^2 + m\vec{v}_A \cdot (\vec{\omega} \times \vec{r}_{G/A})$
Linear impulse-momentum <i>(relating change in velocity to change in time)</i>	particle	$\int_{t_1}^{t_2} \sum \vec{F} dt = m\vec{v}_2 - m\vec{v}_1$
	rigid body <i>(G = c.m.)</i>	$\int_{t_1}^{t_2} \sum \vec{F} dt = m\vec{v}_{G2} - m\vec{v}_{G1}$
Angular impulse-momentum <i>(relating change in angular velocity to change in time)</i>	particle <i>(O = fixed point)</i>	$\int_{t_1}^{t_2} \sum \vec{M}_O dt = \vec{H}_{O2} - \vec{H}_{O1}$ where $\vec{H}_O = m\vec{r}_{P/O} \times \vec{v}_P$
	rigid body <i>(A = fixed point or c.m.)</i>	$\int_{t_1}^{t_2} \sum \vec{M}_A dt = \vec{H}_{A2} - \vec{H}_{A1}$ where $\vec{H}_A = I_A\vec{\omega}$