

Equilibrium:

a) Shaft (3) is free at end D.  $\Rightarrow T_3 = 0$

$$\text{Connector C:} \quad T_3 + 2T - T_2 = 0 \Rightarrow T_2 = 2T \quad (1)$$

$$\text{Connector B:} \quad T_2 - T_1 = 0 \Rightarrow T_1 = T_2 = 2T \quad (2)$$

Where,  $T_1, T_2, T_3$  are the torques carried by the three shafts.

Polar moments are represented here as  $J_i$ . (They can also be denoted as  $I_p$ )

$$\text{b) } \theta_1 = \frac{T_1 L_1}{G_1 J_1} = \frac{(2T)(L)}{(2G)(J_1)} = \frac{32TL}{\pi G d^4}; \quad \theta_2 = \frac{T_1 L_1}{G_1 J_1} = \frac{(2T)(1.5L)}{(G)(J_2)} = \frac{96TL}{65\pi G d^4}$$

, where  $\theta_1, \theta_2$  are rotations between the ends of shafts (1) and (2) respectively. Note that  $\theta_3 = 0$ , since torque carried by shaft (3) is 0.

Compatibility:

$$\theta_A = 0 \quad (\text{wall}) \quad (3)$$

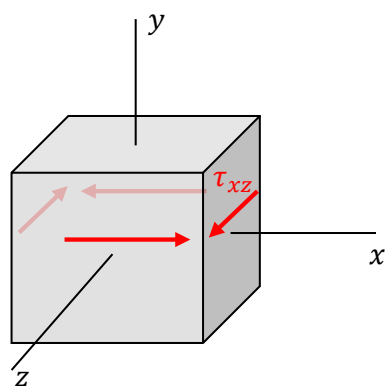
$$\theta_B = \theta_A + \theta_1 = \theta_1 \quad (4)$$

$$\theta_C = \theta_B + \theta_2 = \theta_1 + \theta_2 \quad (5)$$

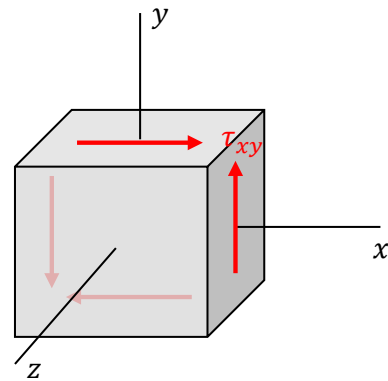
$$\theta_D = \theta_C + \theta_3 = \theta_C \quad (6)$$

From (4):  $\theta_B = \frac{32TL}{\pi Gd^4}$

From (5):  $\theta_C = \theta_B + \theta_2 = \frac{32TL}{\pi Gd^4} + \frac{96TL}{65\pi Gd^4} = \frac{2176}{65} \frac{TL}{\pi Gd^4} = \theta_D$



Element M



Element N