ME 323: Mechanics of Materials

Summer 2024

SOLV TON Homework Set H10

Assigned/Due: June 21/June 25

A shaft system is made up of components (1), (2) and (3), with all three components having solid circular cross-sections and are made up of the same material having a shear modulus of G. Components (1) and (2) have outer diameters of 2d, whereas component (3) has an outer diameter of d. Component (1) is attached to a fixed wall at end B. The three components are joined at the rigid connectors of C and D, as shown. Torques 3T and T are applied to the shaft system as shown.

- a) Determine the torque carried by each shaft component.
- b) Determine the angles of rotation for connectors C, D and H. Include appropriate signs on your answers.
- c) Determine the maximum shear stress in the shaft system. Determine the location(s) of this maximum shear stress in terms of position(s) along the length of the shaft and position(s) on the cross-section.

Express your answers in terms of, at most: *T*, *d*, *G* and *L*.



$$\begin{split} & \bigtriangleup \varphi_{2} = \frac{T_{2}L}{G_{2}T_{p_{2}}} ; \ T_{p_{2}} = \mathcal{I}_{p_{1}} = \frac{T_{2}}{T_{2}}d^{4} \\ & = \frac{2}{T_{1}} \frac{T_{L}}{G_{d}} \\ & \bigtriangleup \varphi_{0} = \frac{T_{3}L}{G_{2}T_{p_{3}}} ; \ T_{p_{3}} = \frac{T_{2}}{T_{2}} \left(\frac{d}{d}\right)^{4} = \frac{T_{1}}{32}d^{4} \\ & = \frac{32}{T_{1}} \frac{T_{L}}{G_{d}} \\ & = \frac{32}{T_{1}} \frac{T_{L}}{G_{d}} \\ & \varphi_{0} = \varphi_{0} + \Delta\varphi_{1} = -\frac{g_{1}}{T_{1}} \frac{T_{L}}{G_{d}} \\ & \varphi_{0} = \varphi_{0} + \Delta\varphi_{2} = -\frac{G_{1}}{T_{1}} \frac{T_{L}}{G_{d}} \\ & \varphi_{0} = \varphi_{0} + \Delta\varphi_{3} = \frac{2G_{1}}{T_{1}} \frac{T_{L}}{G_{d}} \\ & \varphi_{1} = \varphi_{0} + \Delta\varphi_{3} = \frac{2G_{1}}{T_{1}} \frac{T_{L}}{G_{d}} \\ & (\Box_{1}|m_{0x}] = \frac{|T_{1}|(ed/2)}{T_{p_{1}}} = \frac{4}{T_{1}} \frac{T_{1}}{G_{d}} \\ & [T_{2}|m_{0x}] = \frac{|T_{2}|\left(\frac{ed}{2}\right)}{T_{p_{3}}} = \frac{2}{T_{1}} \frac{T_{1}}{G_{3}} \\ & [T_{2}|m_{0x}] = \frac{|T_{2}|\left(\frac{ed}{2}\right)}{T_{p_{3}}} = \frac{1}{T_{1}} \frac{T_{1}}{G_{3}} \\ & [T_{2}|m_{0x}] = \frac{|T_{2}|\left(\frac{ed}{2}\right)}{T_{p_{3}}} = \frac{1}{T_{1}} \frac{T_{1}}{G_{3}} \\ & [T_{2}|m_{0x}] = \frac{|T_{2}|\left(\frac{ed}{2}\right)}{T_{p_{3}}} = \frac{1}{T_{1}} \frac{T_{1}}{G_{3}} \\ & (\Box_{1}|m_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x}|f_{0x$$