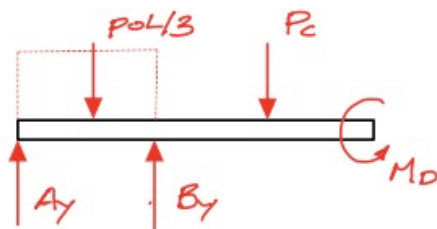


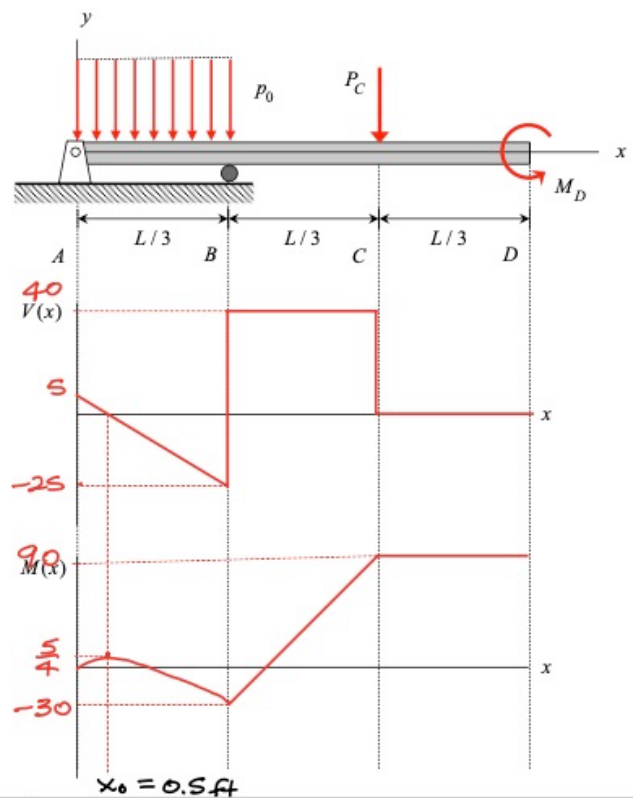
Consider the loading on the beam shown below.

- Determine the reactions at supports A and B.
- Sketch the shear force $V(x)$ and bending moment $M(x)$ distribution on the beam using the axes below. Provide details on your calculations.

Use the following in your calculations: $L = 9\text{ ft}$, $p_0 = 10\text{ kips/ft}$, $P_C = 40\text{ kips}$ and $M_D = 90\text{ ft}\cdot\text{kips}$.



$$\begin{aligned} \bullet \sum M_A &= B_y(3) - (40)(6) - \left[\frac{(10)(9)}{3}\right]\left(\frac{3}{2}\right) + 90 = 0 \\ &\rightarrow B_y = 65\text{ kips} \\ \bullet \sum F_y &= -\frac{(10)(9)}{3} + B_y - 40 + A_y = 0 \\ &\rightarrow A_y = 40 - 65 + 30 = 5\text{ kips} \end{aligned}$$



$$\begin{aligned} V(3^-) &= V(0) + (-10)(3) \\ &= 5 - 30 = -25 \\ V(3^+) &= V(3^-) + B_y = 40 \\ V(x_0) &= V(0) + (-10)x_0 = 0 \\ &\rightarrow x_0 = 0.5\text{ ft} \\ V(6^-) &= V(3^+) = 40 \\ V(6^+) &= V(6^-) - 40 = 0 \\ V(9) &= V(6^+) = 0 \quad \checkmark \text{ (check)} \end{aligned}$$

$$\begin{aligned} M(x_0) &= M(0) + \frac{1}{2}(5)(\frac{1}{2}) = \frac{5}{4} \\ M(3) &= M(x_0) + \frac{1}{2}(-29)(2.5) = -30 \\ M(6) &= M(3) + (40)(3) = 90 \\ M(9) &= M(6) = 90 \quad \checkmark \text{ (check)} \end{aligned}$$