February 23, 2022

INSTRUCTIONS

Begin each problem in the space provided. If additional space is required, use the paper provided to you.

Work appearing on the backside of any exam page will NOT be graded.

If your solution does not follow a logical thought process, it will be assumed to be in error.

PROBLEM No. 1 (25 points)

Problem 1 consists of 10 questions. Each question is worth 2.5 points.

(a) A lighting truss in a theater is suspended from the ceiling by wire ropes. The truss hangs above the audience and is designed to hold 10 lights.

The factor of safety for the wire ropes is most likely:

◯ 1.2

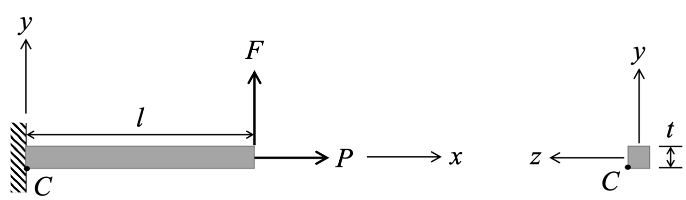
◯ 2

◯ 5

◯ 10

In a few words, justify your answer.

(b) The square cantilevered beam is acted on by loads F and P.



Location C is a state of plane stress.

◯ True

◯ False

(c) The Mohr's circle for a particular state of plane stress is shown below. The part is made of a brittle material.

The factor of safety using the Brittle Coulomb Mohr (BCM) theory is 1.5. The factor of safety using the Modified Mohr (MM) theory is most likely:

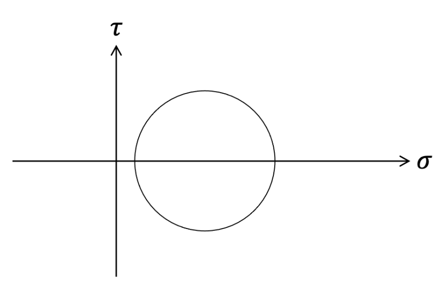
◯ 0.9

◯ 1.3

◯ 1.5

◯ 1.7

◯ 3.1



(d) The Mohr's circle for a particular state of plane stress is shown below. The part is made of a ductile material.

The factor of safety using the Maximum Shear Stress (MSS) theory is 1.5. The factor of safety using the Distortion Energy (DE) theory is most likely:

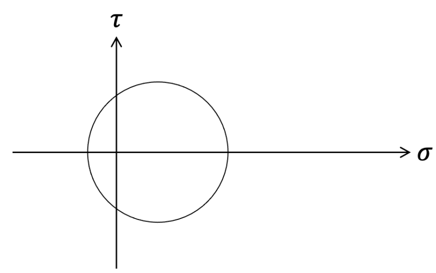
◯ 0.9

◯ 1.3

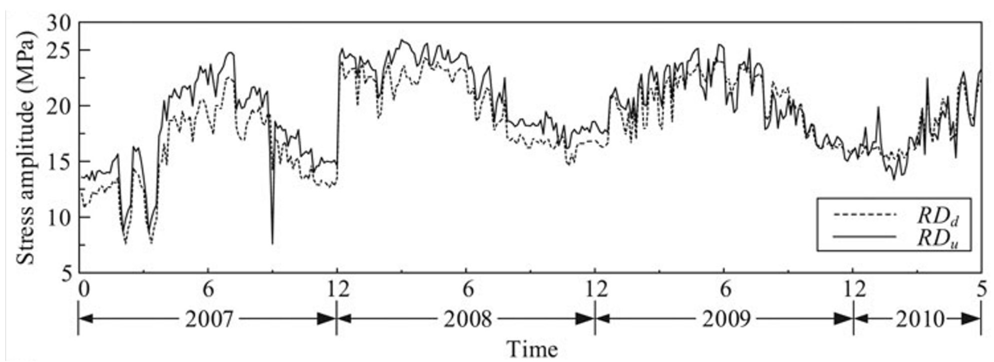
◯ 1.5

◯ 1.7

◯ 3.1



(e) The deck of a bridge is subjected to the stress-time pattern shown below, representing three and a half years of traffic.



The most applicable fatigue method is:

◯ Stress-life

◯ Strain-life

◯ Linear elastic fracture mechanics

In a few words, justify your answer.

(f) A 1-inch diameter rotating steel shaft is loaded in bending. The fully corrected endurance limit is $S_e = 26.5$ kpsi.

The shaft diameter is increased from 1 inch to 1.5 inches. All other conditions are kept the same. The fully corrected endurance limit is now:

○ $S_e = 25.4$ kpsi

○ $S_e = 26.5$ kpsi

○ $S_e = 27.6$ kpsi

○ Cannot be determined from the given information

(g) A colleague hands you a steel part and asks you to quickly calculate the part's factor of safety for infinite life (n_f) using the Goodman criterion.

You cannot tell if the part's surface is ground or machined.

Which surface finish will give you the more conservative prediction for n_f?

○ A ground surface is more conservative.

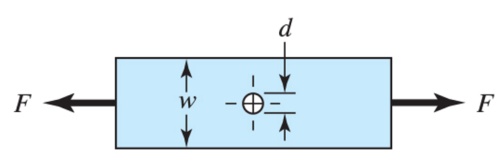
○ A machined surface is more conservative.

In a few words, justify your answer.

(h) A bar with width $w = 10$ inches and thickness $t = 1$ inch includes a transverse hole with diameter $d = 1$ inch. The bar is made of a brittle material and failed when the static load increased to $F = 1000$ lbf.

The hole diameter is increased to $d = 2$ inches, while the bar width, thickness, and material are unchanged.

The static axial load expected to fail the bar is now:



○ $F = 920$ lbf

○ $F = 960$ lbf

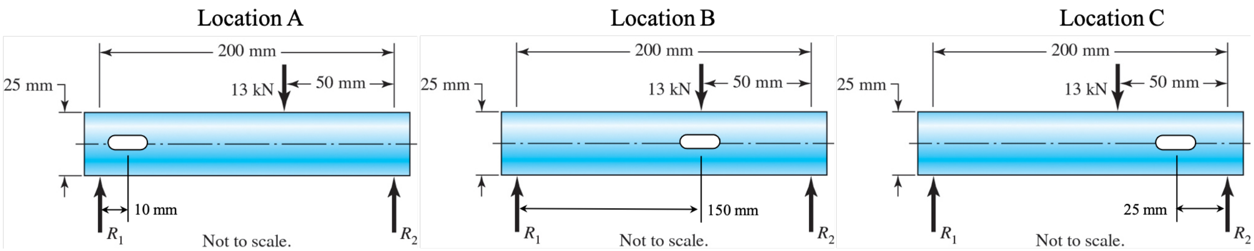
○ $F = 1000$ lbf

○ $F = 1040$ lbf

○ $F = 1080$ lbf

○ Cannot be determined from the given information

(i) A rotating shaft is supported by bearing reaction forces R_1 and R_2 and is loaded with a transverse load of 13 kN as shown in the figure.



You have three options for locating a keyseat on the rotating shaft. Which location is the best option?

◯ Location A
◯ Location B
◯ Location C

(j) A journal bearing is designed with a nominal size of 1.25 inches.

The bushing (hole) diameter dimensions range from 1.2500 in to 1.2525 in.

The journal (shaft) diameter dimensions range from 1.2480 in to 1.2490 in.

The fit is most likely which of the following?

Note: this question can be answered without performing any calculations.

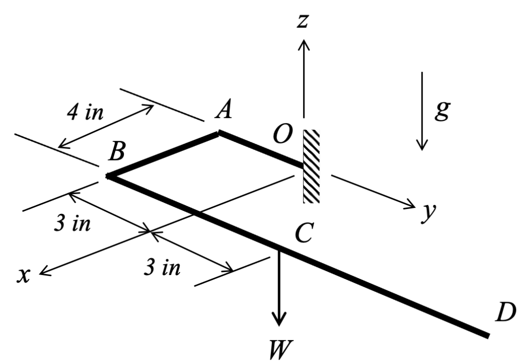
◯ Close running fit
◯ Locational transition fit
◯ Locational interference fit
◯ Medium drive fit
◯ Force fit

PROBLEM No. 2 (25 points)

A paper towel holder is modeled as cantilevered beam $OABCD$. The towel holder is in the xy-plane, where gravity acts in the $-z$-direction.

The towel holder is made of a stainless steel tube with outer diameter $D = 0.5$ inch, wall thickness $t = 0.028$ inch, cross-sectional area $A = 0.0415$ in^2, mass moment of inertia $I = 0.00116$ in^4, and polar moment of inertia $J = 0.00232$ in^4. The yield strength is $S_y = 35$ kpsi.

The weight of the tube is neglected. The weight of the paper towels is modeled as a point load W acting at location C.



Determine the following.

(a) For a cut through segment OA, the internal loads are (select all that apply):

- ◯ Axial compression
- ◯ Axial tension
- ◯ Torsion
- ◯ Bending
- ◯ Transverse shear

(b) For a cut through segment AB, the internal loads are (select all that apply):

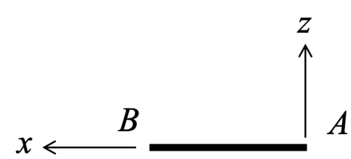
- ◯ Axial compression
- ◯ Axial tension
- ◯ Torsion
- ◯ Bending
- ◯ Transverse shear

(c) For a cut through segment BC, the internal loads are (select all that apply):

- ◯ Axial compression
- ◯ Axial tension
- ◯ Torsion
- ◯ Bending
- ◯ Transverse shear

PROBLEM No. 2 (continued)

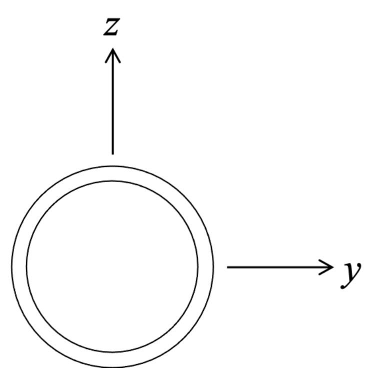
(d) Identify the critical cross-section on segment AB. Clearly show the location on the figure below. Justify your choice.



(e) Identify the critical element(s) on the critical cross-section identified in part (d).

— Clearly show the location(s) of the critical element(s) on the sketch below.

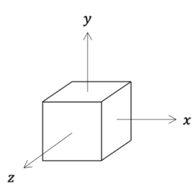
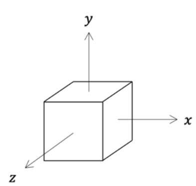
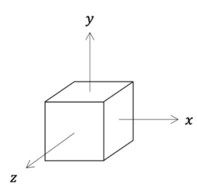
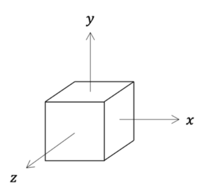
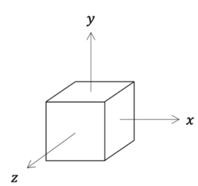
— Justify your choice(s). You may use the attached Stress Analysis Worksheet to aid your analysis.



(f) For the critical element(s) identified in part (e), determine the factor of safety using the distortion energy failure theory. A roll of paper towels weighs $W = 0.6$ lbf.

PROBLEM No. 2 (continued)

- Draw the machine component's critical cross-section.
- Identify and label the potential locations for the critical element(s) (e.g., top, bottom, right, left, and center)

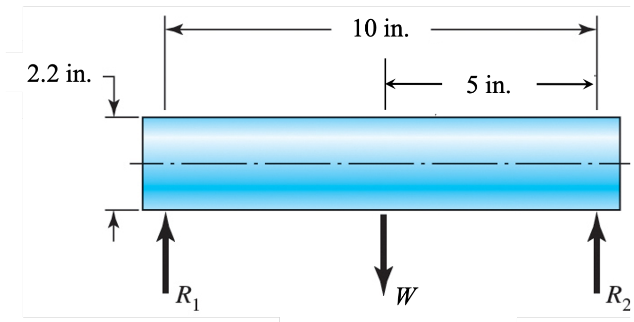
Potential location of critical element						
Internal load	Axial					
	Torsion					
	Transverse shear					
	Bending					
Stress element						

PROBLEM No. 3 (25 points)

A hollow shaft is made of AISI 1050 CD steel. The shaft's outer diameter is $D = 2.2$ inches and inner diameter is $d = 1.6$ inches. The cross-sectional area $A = 1.79$ in^2, mass moment of inertia $I = 0.828$ in^4, and polar moment of inertia $J = 1.656$ in^4.

The shaft rotates at a constant speed and is supported by bearing reaction forces R_1 and R_2.

The shaft operates in an environment where the temperature is 600°F. Weight W acts at the location shown in the diagram below. The desired reliability is 90%.



Determine the following.

(a) The estimated endurance limit S_e'.

(b) The fully corrected endurance limit S_e.

(c) The fatigue strength of the shaft at 1000 cycles.

(d) The maximum weight W for the rotating shaft to achieve a life of $N = 100,000$ cycles with a factor of safety of $n = 1$.

PROBLEM No. 3 (continued)

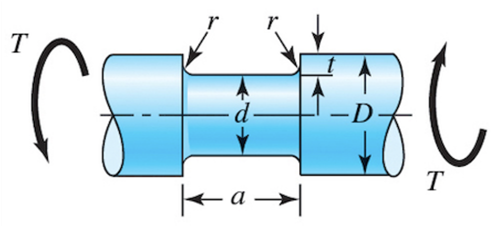
PROBLEM No. 4 (25 points)

The rotating round shaft with a flat-bottom groove is loaded with a torque T that varies between T_{min} and T_{max}, where T_a and T_m are related by:

$$\frac{T_a}{T_m} = 0.5$$

The shaft's dimensions are $r = 1.0$ mm, $t = 10$ mm, $a = 25$ mm, $d = 20$ mm, and $D = 40$ mm.

The shaft has ultimate tensile strength $S_{ut} = 700$ MPa and yield strength $S_y = 590$ MPa. The fully corrected endurance limit is $S_e = 170$ MPa.



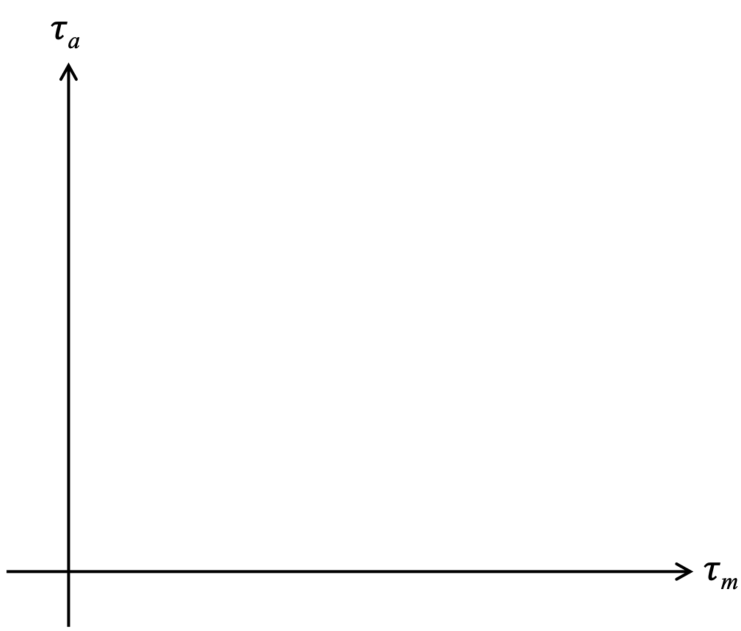
Determine the following.

(a) The fatigue stress concentration factor K_{fs}.

(b) T_{min} and T_{max} for the rotating shaft such that the factor of safety for infinite life found with the Goodman criterion is $n_f = 2$.

(c) Check for first-cycle yielding.

(d) Sketch and label the stress state on a fluctuating-stress diagram using the axes provided. Show the Goodman line, the yield line, and the zones for infinite life, finite life, and first-cycle yielding.



PROBLEM No. 4 (continued)

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