ution

INSTRUCTIONS:

This quiz is open-book, open-note, and you may work with your classmates.

GIVEN:

The AISI 1030 hot rolled steel shaft is rotating at a constant speed in the simply supported bearings at points O and E.

The shaft has yield strength $S_y = 37.5$ kpsi, ultimate tensile strength $S_{ut} = 68$ kpsi, and a fully-corrected endurance limit of $S_e = 18.3$ kpsi.

The two constant diameters of the stepped shaft are D = 2 in and d = 1.2 in.

The constant vertical load at location C is $F_C = 225$ lbf and the shaft transmits a constant torque T = 150 lbf-in.

The fatigue stress concentration factors at the step are $K_f = 3$ for bending and $K_{fs} = 2.5$ for torsion.



FIND:

- a) Sketch diagrams showing the internal loads (bending and torsion) acting on the rotating shaft.
- b) Identify the critical cross-section of the shaft.
- c) For a point on the circumference of the shaft at the critical cross-section, sketch the bending stress as a function of time.
- d) For a point on the circumference of the shaft at the critical cross-section, sketch the torsional shear stress as a function of time.
- e) The factor of safety for infinite life using the Goodman criterion.
- f) The factor of safety for yielding.



∑M0=0 12·RE - 8·225=0 → RE= 150 16f ∑Fy=0 Fo + RE-225=0 → Fo=225-150=75 16f



b) critical cross-section is at B due to relatively high bending moment and stress raiser.

c)
$$r$$

bending stress
is emplotely
 $me = 3 \cdot \frac{1}{2} = \sqrt{3} \cdot 2.5 \cdot \frac{150}{32} (1.2 \ln)^{1}$
 $reversed
 $reversed$
 $reversed
 $reversed$
 $revers$$$

$$\frac{1}{n_f} = \frac{7.957}{18.3} + \frac{1.914}{68} \rightarrow n_f = 2.1$$

f)
$$n_y = \frac{S_y}{\sigma_a' + \sigma_m'} = \frac{37.5 \text{ kpsi}}{7.957 + 1.914} = 3.8 = n_y$$