

### Conceptual Question C5.1

**Given:** A rigid body is acted upon by a set of four forces. It is desired to represent this set of forces (System I) by an equivalent force-couple system (System II) at point A on the body:  $\vec{R} = R_x\hat{i} + R_y\hat{j}$  and  $\vec{M} = M\hat{k}$ .

**Find:**

Circle the correct response below regarding the  $x$ -component of the resultant  $\vec{R}$ :

- $R_x < 0$
- $R_x = 0$
- $R_x > 0$

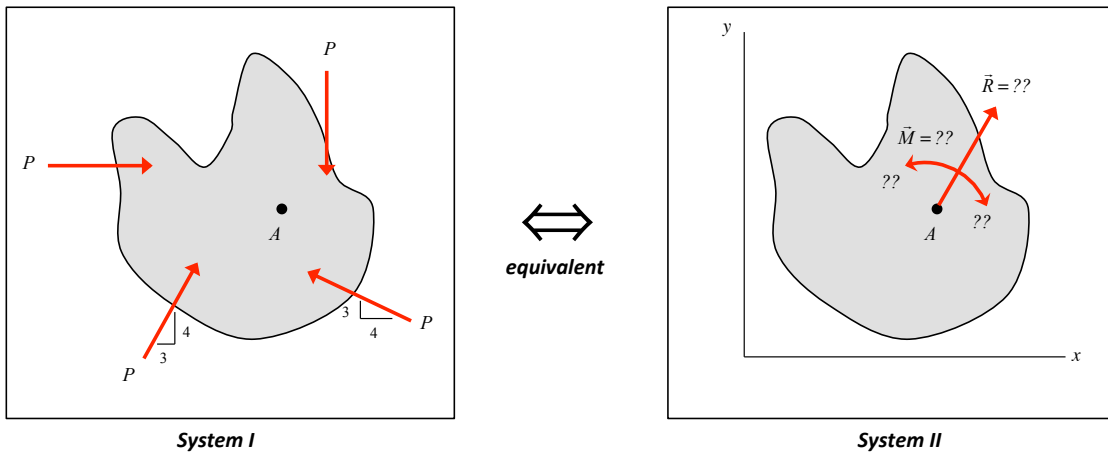
Circle the correct response below regarding the  $y$ -component of the resultant  $\vec{R}$ :

- $R_y < 0$
- $R_y = 0$
- $R_y > 0$

Circle the correct response below regarding the direction of the couple  $\vec{M}$ :

- $\vec{M}$  is counter-clockwise
- $\vec{M} = 0$
- $\vec{M}$  is clockwise

Provide explanations for your answers.

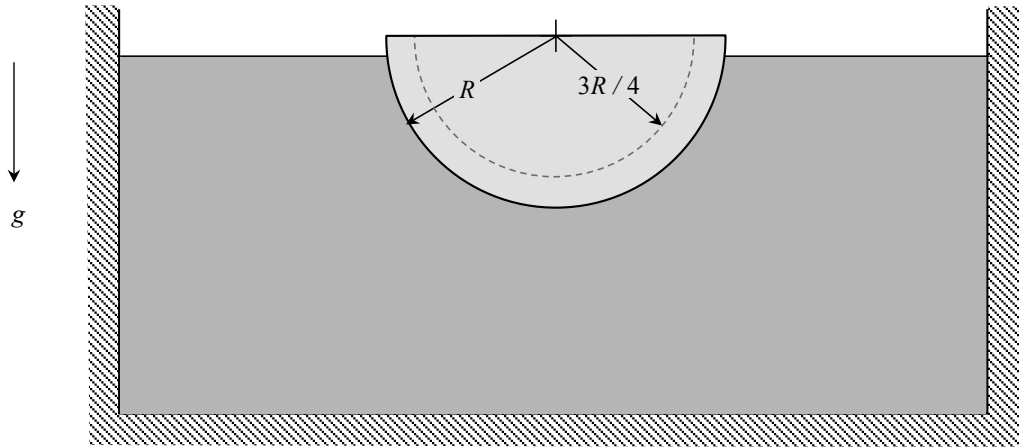


### Conceptual Question C5.2

**Given:** A hemispherical shell cap with an outer radius of  $R$  and inner radius of  $3R/4$  is made of a material having a mass density of  $\rho_c = 2\rho_w$ , where  $\rho_w$  is the mass density of water.

**Find:** Will the cap float when placed in water in the orientation shown below?

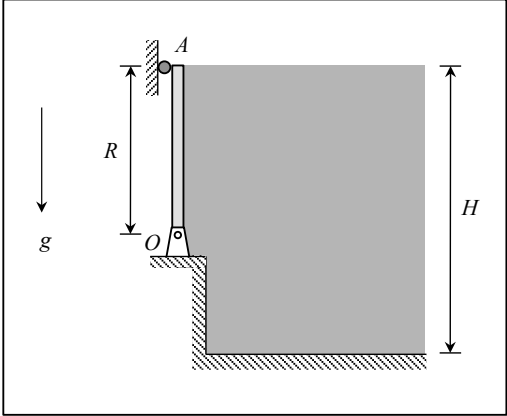
Provide an explanation for your answer.



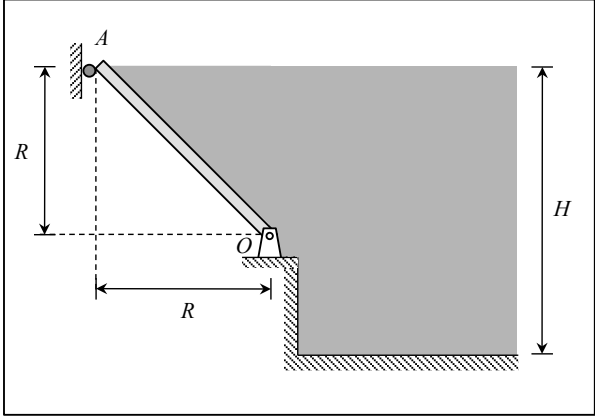
**Conceptual Question C5.3**

**Given:** Consider the vertical Gate 1 shown below that is holding back water of density  $\rho_w$ . Gate 2, also shown below, is mounted with an inclined orientation. Each gate has a dimension of  $b$  into the page. The weights of the gates are to be considered negligible compared to the weight of the water being held back by the gates. Let  $(N_A)_1$  and  $(N_A)_2$  represent the reaction forces acting at ends A of Gates 1 and 2, respectively.

**Find:** Determine the ratio of  $(N_A)_2 / (N_A)_1$ .



Gate 1

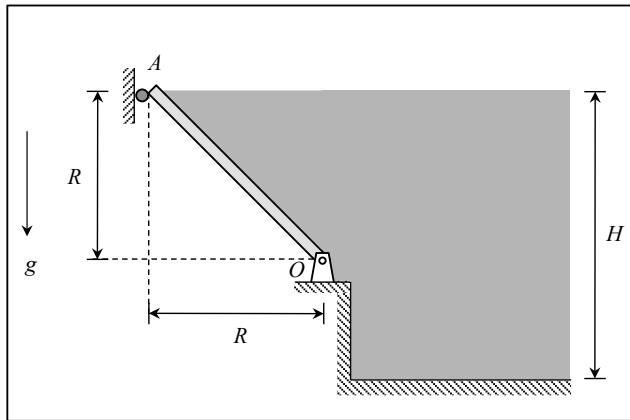


Gate 2

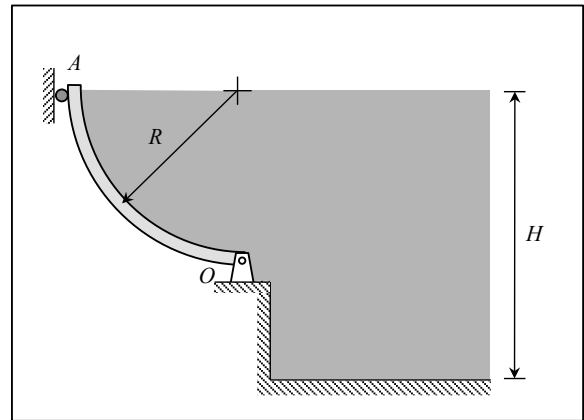
### Conceptual Question C5.4

**Given:** Consider the straight, inclined Gate 1 shown below that is holding back water of density  $\rho_w$ . Gate 2, also shown below, is a quarter circle arc. Each gate has a dimension of  $b$  into the page. The weights of the gates are to be considered negligible compared to the weight of the water being held back by the gates. Let  $(N_A)_1$  and  $(N_A)_2$  represent the reaction forces acting at ends A of Gates 1 and 2, respectively.

**Find:** Determine the ratio of  $(N_A)_2 / (N_A)_1$ .



Gate 1

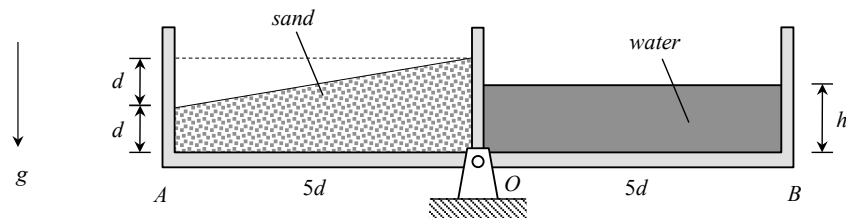


Gate 2

### Conceptual Question C5.5

**Given:** A box containing sand is mounted on a lever between A and O. Let  $\rho_s$  represent the mass density of the sand. A second box is mounted between O and B on the same lever. This second box is to be filled with water (having a mass density of  $\rho_w$ ) to a height  $h$  that will keep the lever in balance. Use  $\rho_s = 2\rho_w$ . Each box has a dimension of  $b$  into the page. The weights of the boxes and the lever can be considered negligible as compared to the sand and water.

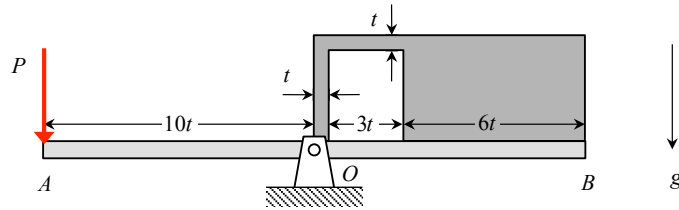
**Find:** Determine the height  $h$  of the water that is needed to balance the sand. Express your answer in terms of  $d$ .



### Conceptual Question C5.6

**Given:** A body having a weight of  $W$  is placed between  $O$  and  $B$  on a lever. A vertical force  $P$  acts at end  $A$  of the lever. The weight of the lever is to be considered to be negligible compared to the weight of the body.

**Find:** Determine the force  $P$  required to keep the lever in balance. Express your answer in terms of  $W$ .

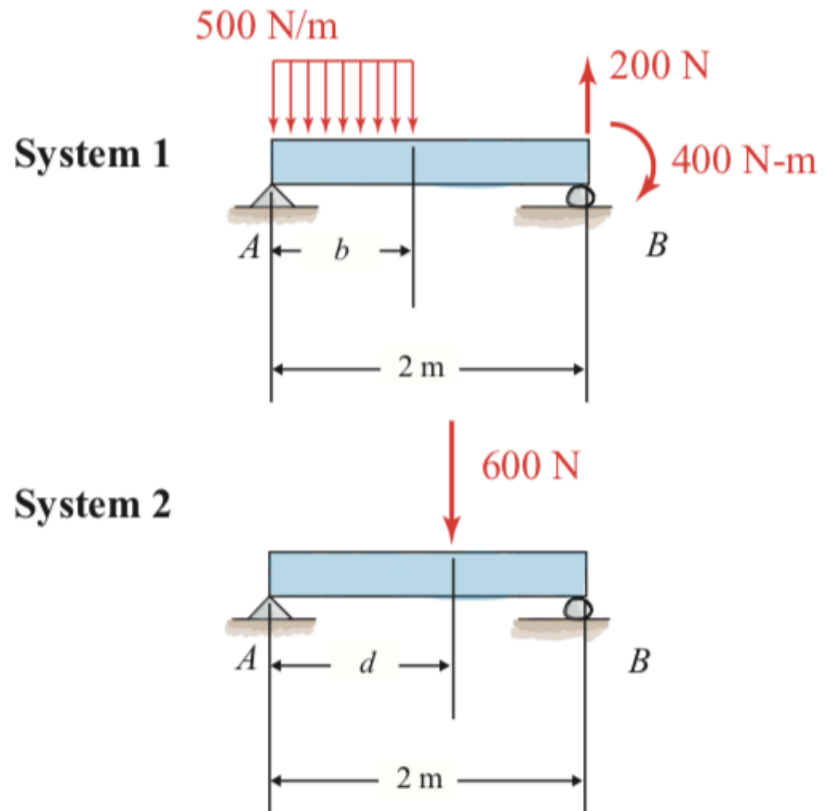


### Conceptual Question C5.7

**Given:** Consider the two statically-equivalent force systems shown below.

**Find:** For this problem:

- Determine the length  $b$  over which the line load acts.
- Determine the location  $d$  of the single equivalent force.

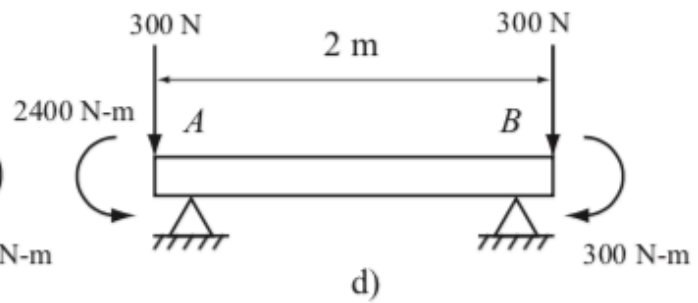
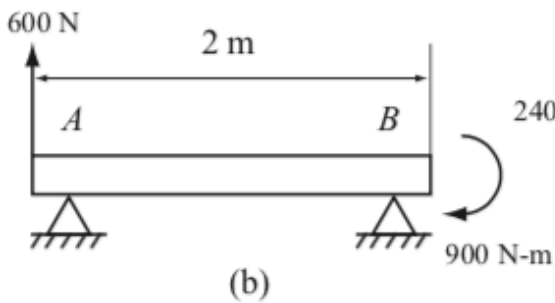
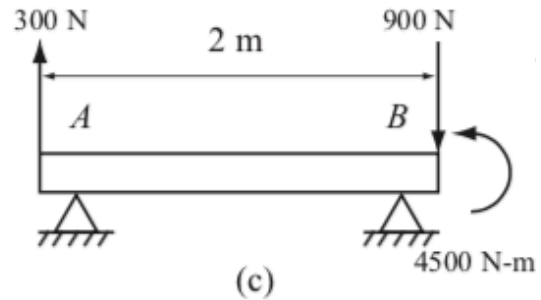
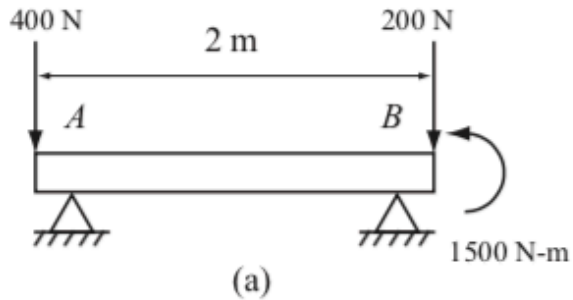


### Conceptual Question C5.8

**Given:** Consider the four different load systems (a)-(d) shown below.

**Find:** For this problem:

- For each loading system, determine the equivalent force-couple system at location A.
- Which of the loading systems, if any, are equivalent?



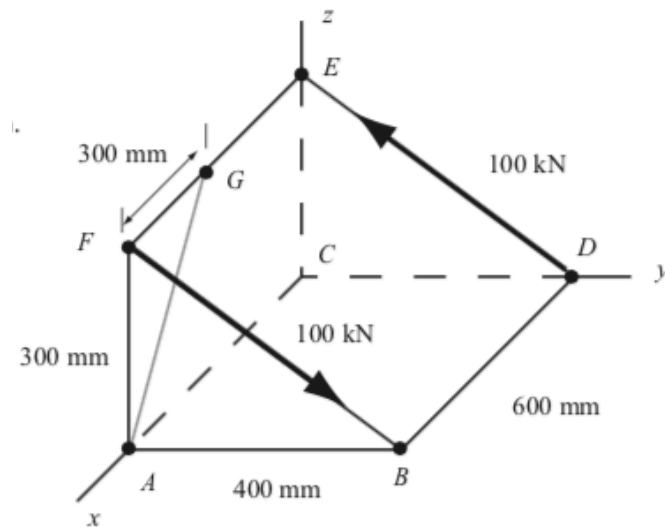


### Conceptual Question C5.9

**Given:** Consider the load pair shown below.

**Find:** For this problem:

- Determine the equivalent force-couple system for this load pair. Where does this equivalent system act?
- Determine the component of the couple found above along line segment AG.

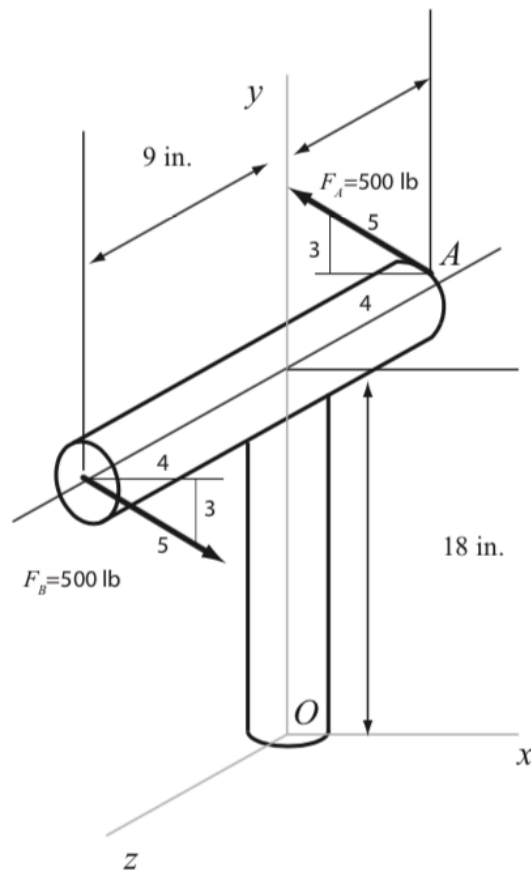


### Conceptual Question C5.10

**Given:** Consider the load pair acting on the T-shaped bracket shown below.

**Find:** For this problem:

- Determine the resultant moment acting about point  $O$  due to the pair of forces  $F_A$  and  $F_B$  on the bracket.
- Determine moment of the load  $F_B$  about point  $A$ .
- Determine moment of the load  $F_A$  about point  $B$ .
- Compare your results from above.

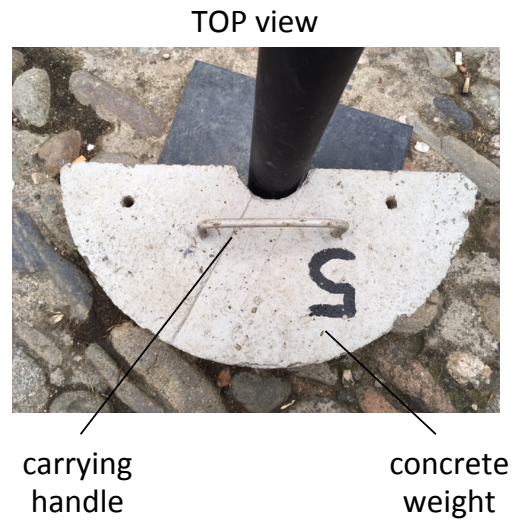
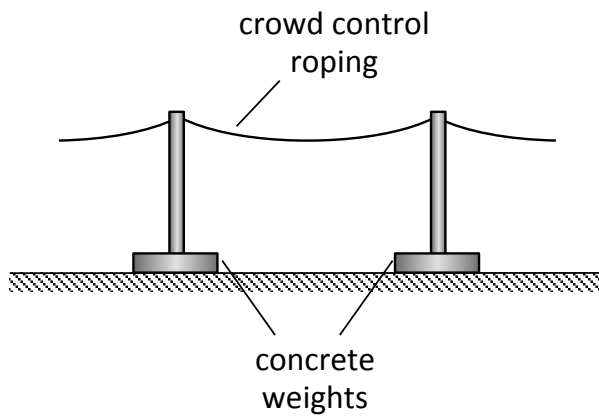


### Conceptual Question C5.11

**Given:** Supports for crowd control roping are held in place by semi-circular concrete weights, as shown below. Built into these concrete weights are handles for transportation purposes.

**Find:** Consider the location of these handles on the weights.

- Where is the optimal location for these handles on the weights for balance during carrying?
- Based on the photo shown below right, how close are the handles to their optimal location?



### Conceptual Question C5.12

**Given:** During live and video-recorded performances of the song "Criminal Minds," the late Michael Jackson and his dance team included a "45 degree lean" as part of their dance moves.

**Find:** Consider the approximate location of the center of mass of the human body shown below.

- What makes this dance move appear so impressive (and physics defying)?
- How did Mr. Jackson and his team perform this move?

